

SET - I
SUMMATIVE ASSESSMENT - II - 2016 - 2017
MATHEMATICS
(English Medium)

Class : IX(P-1)

(Max. Marks : 40)

PART - A
SECTION - I

4 x 2 = 8

1. Surface Area of Sphere = $4\pi r^2$

(½m)

$$4\pi r^2 = 616$$

$$4 \times \frac{22}{7} \times r^2 = 616$$

$$r^2 = \frac{616 \times 7}{4 \times 22} \Rightarrow r = 7$$

(½m)

$$\therefore \text{radius} = 7\text{cm}$$

2. Four angles of Quadrilateral 2x, 4x, 5x, 7x, 8x

$$2x + 4x + 5x + 7x = 360^\circ$$

$$18x = 360^\circ, \Rightarrow x = 20^\circ$$

(½m)

$$\therefore \text{Angles of Quadrilateral are } 40^\circ, 80^\circ, 100^\circ, 140^\circ$$

(½m)

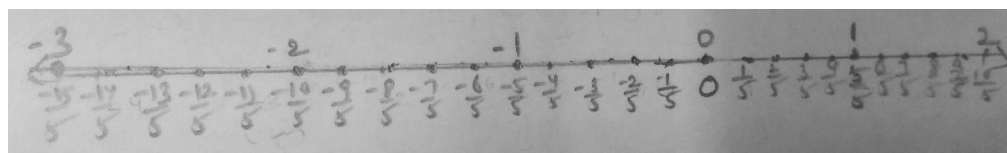
3. S.A.S congruence rule :-

Two triangles are congruent if two sides and the included angle of one triangle are equal to the two sides and included angle of the other triangle (1m)

4. Divide each unit into five equal parts to the right and left sides of zero on the number

line. Take 13 parts left side of the zero if represents $\frac{13}{5}$ (1m)

(1m)



SECTION - II

5x4 = 20

5. Volume of the cylinder (V) = 308cm^3

$$\pi r^2 h = 308$$

$$\text{height}(h) = 8\text{cm}$$

$$\frac{22}{7} \times r^2 \times 8 = 308$$

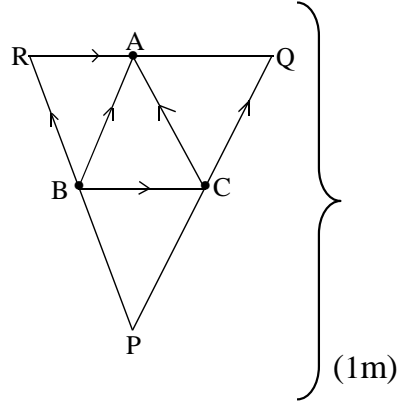
$$r^2 = \frac{308 \times 7}{22 \times 8} = \frac{49}{4}$$

$$\therefore r = \sqrt{\frac{49}{4}} = \frac{7}{2}\text{cm}$$

(1m)

$$\begin{aligned}
 & 2\pi r(h) \\
 & = 2 \times \frac{22}{7} \times \frac{7}{2} \left(\frac{7}{2} + 8 \right) \\
 \text{Total surface Area} & = 22 \left(\frac{7+16}{2} \right) = 22 \times \frac{23}{2} \\
 & = 253 \text{ cm}^2
 \end{aligned}
 \tag{1m}$$

6. $AB \parallel QP$ and $BC \parallel RQ$. So $AB \parallel CQ$ is a $(ABCQ)$ Parallelogram. Similar $BCAR$, $ABPC$ are parallelogram,
 $\therefore BC = AQ$ and $BC = RA$
 A is the mid point of QR
 Similar B and C are mid points of PR and PQ respectively



$$\begin{aligned}
 \therefore AB &= \frac{1}{2} PQ, \quad BC = \frac{1}{2} QR \quad \text{and} \quad CA = \frac{1}{2} PR \\
 \therefore \text{Perimeter of } \triangle PQR &= PQ + QR + PR \\
 &= 2AB + 2BC + 2CA \\
 &= 2(AB + BC + CA) \\
 &= 2(\text{Perimeter of } \triangle ABC)
 \end{aligned}
 \tag{1/2m}$$

$$\therefore \text{The ratio of Perimeter of } \triangle PQR \text{ and } \triangle ABC = 2:1
 \tag{1/2m}$$

7. Suppose, units digits represented by 'x' and tens digit represented by 'y', then the number is $10y + x$ (1/2m)

If we reverse the digits then the new number would be $10x + y$ (1/2m)

$$\therefore \text{Sum of two digit number and reverse the digits number} = 165$$

$$\therefore 10y + x + 10x + y = 165
 \tag{1/2m}$$

$$11x + 11y = 165$$

$$\therefore x + y = 15 \text{ is the required linear equation}
 \tag{1/2m}$$

8. $x + y + 2 = 0$
 $x + y = -2 \rightarrow (1)$ (1/2m)

$$\text{cubins on both sides, we get } (x+y)^3 = (-2)^3$$

$$x^3 + y^3 + 3xy(x+y) = -2^3
 \tag{1/2m}$$

$$x^3 + y^3 + 3xy(-2) = -2^3$$

$$(\because x + y = -2)
 \tag{1/2m}$$

$$x^3 + y^3 + 3xyz = -2^3$$

$$\therefore x^3 + y^3 + z^3 = 3xyz, \text{ Hence proved}
 \tag{1/2m}$$

9. Let

$$\angle ADB = x$$

In $\triangle ACD$, $AC = CD$

$$= \angle CAD = \angle CDA = x \text{ and}$$

Exterior of $\angle ACB = \angle CAD + \angle CDA$

$$= x + x = 2x$$

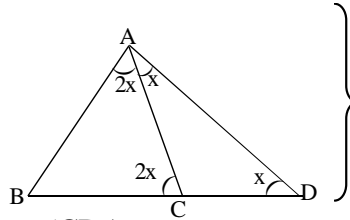
In $\triangle ABC$, $\angle BAC = \angle ACB = 2x (\therefore AB = BC)$

$$\angle BAD = \angle BAC + \angle CAD$$

$$= 2x + x = 3x$$

$$\therefore \text{The ratio of } \angle \text{BAD and } \angle \text{ADB} = 3x : x$$

$$\therefore \angle \text{BAD} : \angle \text{ADB} = 3 : 1$$



(1/2m)

(1/2m)

(1/2m)

(1/2m)

SECTION - III

4x8 = 32

10-A In $\triangle PQR$, $PS \perp QR$, since $\triangle PQS \cong \triangle PRS$

By the CPCT

$PQ = PR$ and $QS = SR$

$$2x+3 = 3y+1 \text{ and } x = y+1$$

$$\Rightarrow 2x-3y = -2 \rightarrow (1) \text{ and } x-y = 1 \rightarrow (2)$$

substitutions $x = y+1$ in (1) we get

$$2(y+1) - 3y = -2$$

$$2y+2 - 3y = -2$$

$$-y = -4 \Rightarrow y = 4$$

substitution $y = 4$ in $x = y+1$

$$x = 4+1 = 5$$

$$\therefore \text{PQR} = x + y + 1 = 5+4+1 = 10 \text{ units}$$

$$PQ = PR = 2(5)+3 = 13 \text{ units, } QS = x = 5 \text{ units}$$

$\triangle PQS$ is right angle

by the pythagoriosis theorem $PQ^2 = QS^2 + PS^2$

$$PS^2 = PQ^2 - QS^2$$

$$= (13)^2 - (5)^2$$

$$= 169 - 25$$

$$PS^2 = 144 \Rightarrow PS = \sqrt{144} = 12 \text{ units}$$

(1m)

(1m)

(1m)

$$\therefore \text{Area of } \triangle \text{PQR} = \frac{1}{2} \times \text{QR} \times \text{PS}$$

$$= \frac{1}{2} \times 10 \times 12$$

$$= 60 \text{ Sq. units}$$

(1m)

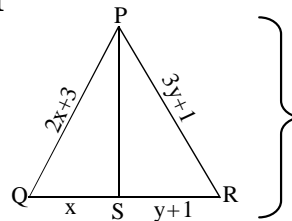
10-B Height of a conical tent (h) = 9m

Diameter of the base (d) = 24m

$$\text{radius (r)} = \frac{d}{2} = \frac{24}{2} = 12m$$

C.S.A of the cone = $\pi r l$

(1m)



$$\left. \begin{aligned} \text{Where } l &= \sqrt{r^2 + h^2} \\ &= \sqrt{12^2 + 9^2} = \sqrt{144 + 81} = \sqrt{225} = 15\text{m} \end{aligned} \right\} \quad (1\text{m})$$

$$\left. \begin{aligned} \text{C.S.A} &= \pi r l \\ &= \frac{22}{7} \times 12 \times 15 \text{sq.m} \end{aligned} \right\} \quad (1\text{m})$$

$$\left. \begin{aligned} \text{cost of canvas per sq.m} &= \text{Rs. } 14 \\ \text{Total cost of the canvas cloth} &= \frac{22}{7} \times 12 \times 15 \times 14 \\ \text{Rs. } &7920.00 \end{aligned} \right\} \quad (1\text{m})$$

11-A The rationalism factor of $7 - 4\sqrt{3}$ is $7 + 4\sqrt{3}$ and the rationalism factor of $\sqrt{3} - 2$ is $\sqrt{3} + 2$ } (1m)

$$\left. \begin{aligned} \frac{1}{7-4\sqrt{3}} + \frac{1}{\sqrt{3}-2} &= \frac{1}{7-4\sqrt{3}} \times \frac{7+4\sqrt{3}}{7+4\sqrt{3}} + \frac{1}{\sqrt{3}-2} \times \frac{\sqrt{3}+2}{\sqrt{3}+2} \\ &= \frac{7+4\sqrt{3}}{(7)^2 - (4\sqrt{3})^2} + \frac{\sqrt{3}+2}{(\sqrt{3})^2 - (2)^2} \\ &= \frac{7+4\sqrt{3}}{49-48} + \frac{\sqrt{3}+2}{3-4} \\ &= \frac{7+4\sqrt{3}}{1} + \frac{\sqrt{3}+2}{(-1)} \\ &= 7+4\sqrt{3} = \sqrt{3}-2 = 5+3\sqrt{3} \end{aligned} \right\} \quad (1\frac{1}{2}\text{m})$$

$$\left. \begin{aligned} \therefore \frac{1}{7-4\sqrt{3}} + \frac{1}{\sqrt{3}-2} &= a+b\sqrt{3} = 5+3\sqrt{3} \\ \therefore a=5, b=3 \end{aligned} \right\} \quad (\frac{1}{2}\text{m})$$

$$\left. \begin{aligned} a^3+b^3 &= (5)^3+(3)^3 \\ &= 125+27 = 152 \end{aligned} \right\} \quad (1\text{m})$$

11-B Thickness of disc = 5mm, $\frac{5}{10}$ cm = 0.5cm

Radius of the disc = 3.5cm

curved surface area of cylinder = 462cm

$$\therefore 2\pi rh = 462 \rightarrow (i)$$

Let the no. of discs = x

Height of the cylinder = h

$$\begin{aligned} &= \text{thickness of disc X no. of discs} \\ &= 0.5x \end{aligned}$$

$$\therefore 2\pi rh = 2 \times \frac{22}{7} \times 3.5 \times 0.5x \rightarrow (ii)$$

by (i) & (ii) , $2 \times \frac{22}{7} \times 3.5^{0.5} \times 0.5x = 462$

$$\therefore x = \frac{462}{2 \times 22 \times 0.5 \times 0.5} = \frac{462}{11} = 42$$

$$\therefore \text{No. of discs} = 42$$

12-A Given :- ABCD Quadrilateral, E,F,G and H are mid points of AB,BC,CD and DA

RTP : EFGH is a parallelogram

Proof: Join \overline{AC} and BD, In $\triangle ABC$. E,F are the mid points of sides AB and BC

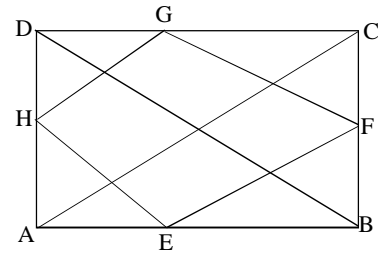
$$\therefore \overline{EF} \parallel \overline{AC} \text{ and } EF = \frac{1}{2} AC \text{ (by the mid point theorem)}$$

$$\text{Also in } \triangle ACD, \overline{HG} \parallel \overline{AC} \text{ and } HG = \frac{1}{2} AC$$

$$\therefore \overline{EF} \parallel \overline{HG} \text{ and } EF = HG$$

Now in EFGH, $EF = HG$ and $EF \parallel HG$

\therefore EFGH is a parallelogram



12-B Let $f(x) = px^2 + 5x + r$ as

$$x - 2 \text{ and } x - \frac{1}{2} \text{ are factors of } f(x)$$

$$\text{then } f(2) = 0 \text{ and } f\left(\frac{1}{2}\right) = 0$$

$$\therefore f(2) = P(2)^2 + 5(2) + r = 0$$

$$= 4p + 10 + r = 0$$

$$\Rightarrow 4P + r = -10 \rightarrow (1)$$

$$\therefore f\left(\frac{1}{2}\right) = p\left(\frac{1}{2}\right)^2 + 5\left(\frac{1}{2}\right) + r = 0$$

$$= \frac{p}{4} + \frac{5}{2} + r = 0$$

$$= p + 10 + 4r = 0$$

$$= p + 4r = -10 \rightarrow (2)$$

From (1) and (2)

$$4P + r = P + 4r$$

$$4P - p = 4r - r$$

$$3P = 3r$$

$$\therefore P = r$$

Hence proved

13-A The given equation is $2x+3y = 12$

X	0	6
Y	4	0

(1m)

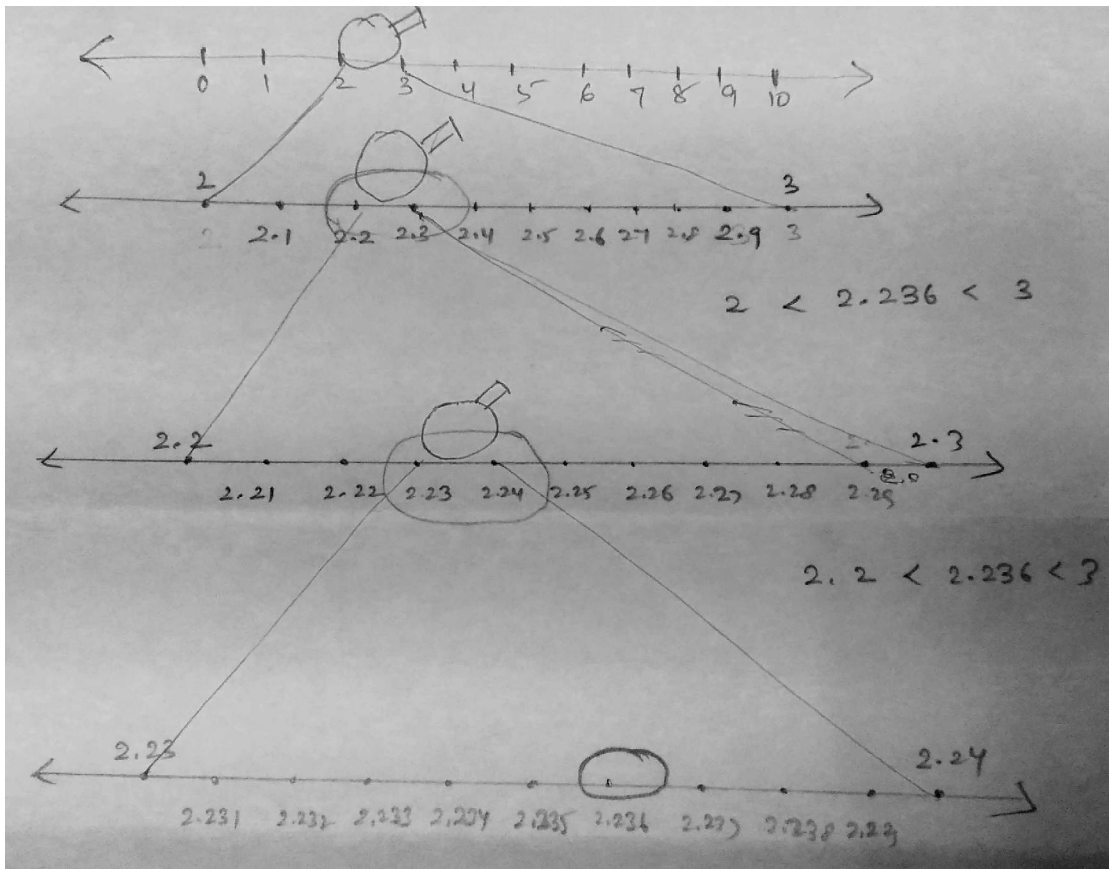
(Drawn the graph)

(2m)

- (i) From the graph when $y = 2$ then $x = 3$ Solutes is $(3,2)$ }
 (ii) From the graph $x = -3$, then $y = 6$ solutes is $(-3,6)$ } (1m)

OR

13-B Value of $\sqrt{5}$ upto 3 decimals is 2.236



PART - B
SECTION - IV

- | | | | | | |
|--------|-------|-------|-------|-------|-------|
| 14 (B) | 15(C) | 16(B) | 17(A) | 18(C) | 19(A) |
| 20(A) | 21(C) | 22(D) | 23(B) | 24(C) | 25(B) |
| 26(A) | 27(C) | 28(B) | 29(B) | 30(B) | 31(B) |
| 32(C) | 33(D) | | | | |